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## Simulating multi-star systems using Python (and maybe C++)

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# Table of contents

- 1 Multi-star simulations
- 2 Sequential Execution
- 3 Parallel Execution
- 4 Parallel Performance and Scaling
- 5 Conclusion and Future Plan

# Outline

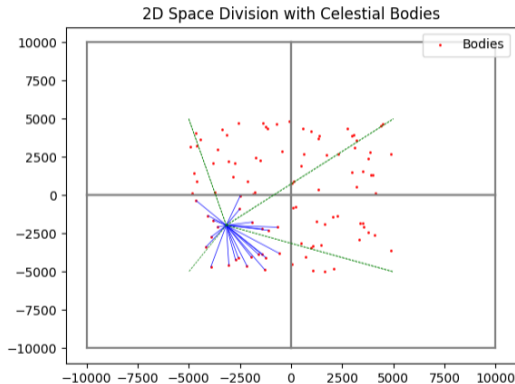
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## Why hard?

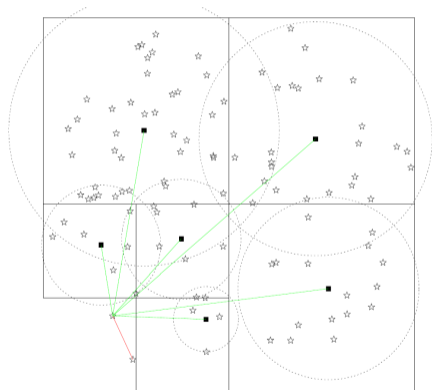
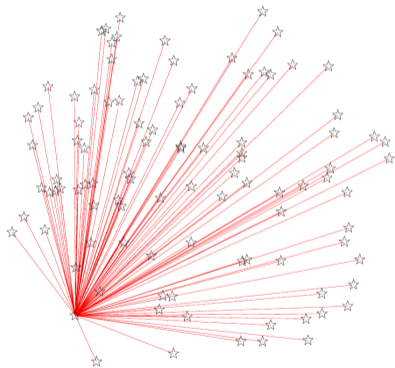
- Simulation is a model of the real world
- Simulation is always approximate, but must give insights
- Simulating real system on a classical computer takes too much time

# Approaches

- Body-body interactions
  - ▶ Complexity  $O(n^2)$
  - ▶ 1M bodies - 1T calculations
- OctTree based object distribution
  - ▶ Complexity  $O(n \log(n))$
  - ▶ 1M bodies - 6M calculations
- Space chunking - Current choice
  - ▶ Complexity  $O(n\sqrt{n})$
  - ▶ 1M bodies - 2B calculations

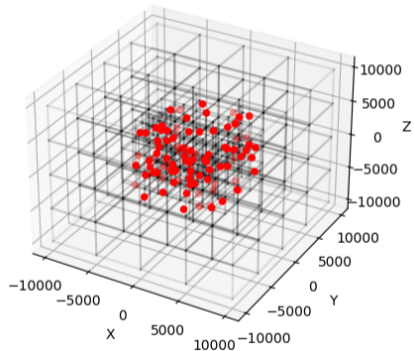


# Body-body vs Tree

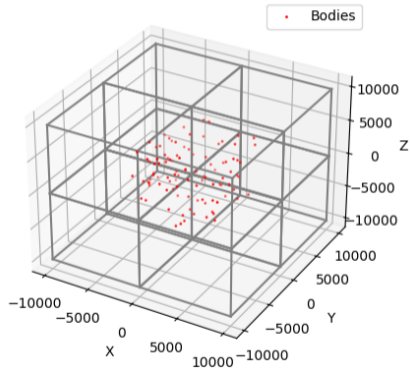


Dehnen and Read, "N-body simulations of gravitational dynamics"

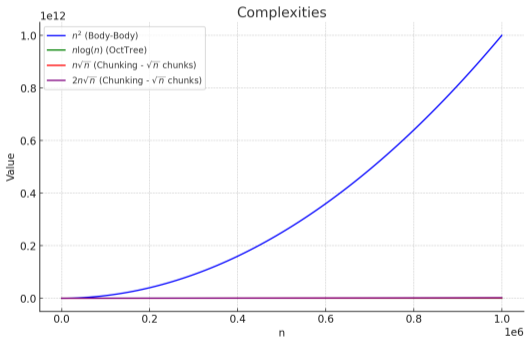
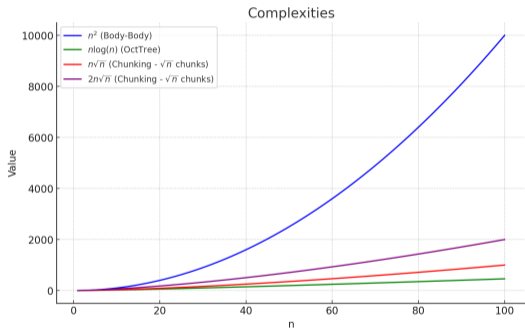
# OctTree vs Space Chunking



3D Space Division with Celestial Bodies



# Complexities



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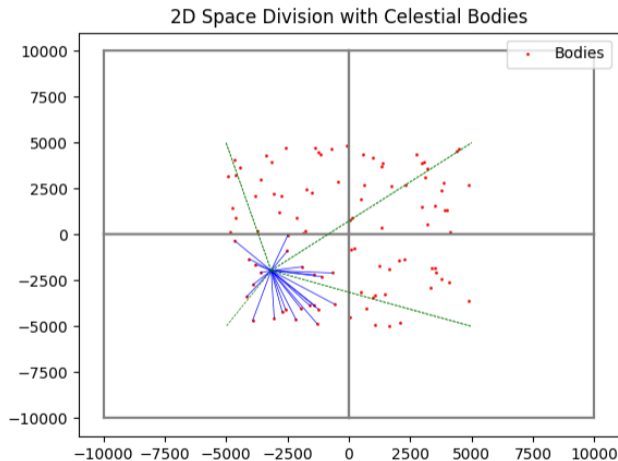
# Calculations

- Same calculation, as in case of an OctTree
- Leapfrog Integrator [1]:

- ▶  $v_{i+0.5} = v_i + a_i * \frac{dt}{2}$

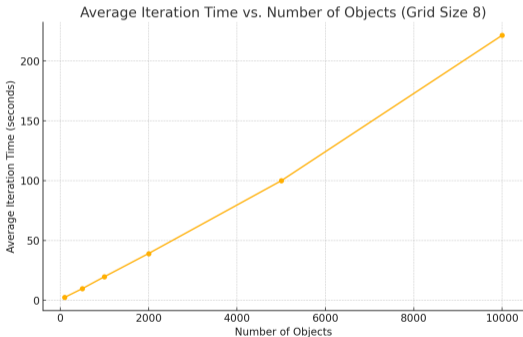
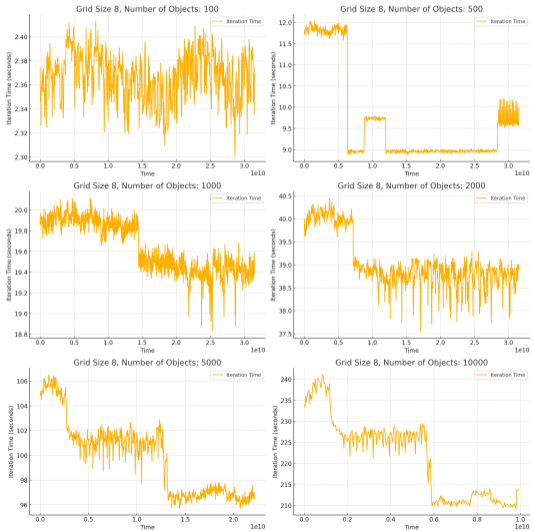
- ▶  $x_{i+1} = x_i + v_{i+0.5} * dt$

- ▶  $v_{i+1} = v_{i+0.5} + a_{i+0.5} * \frac{dt}{2}$

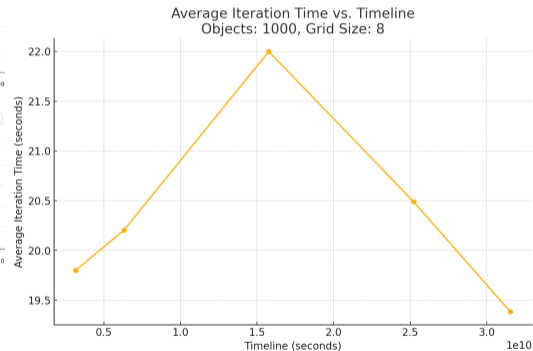
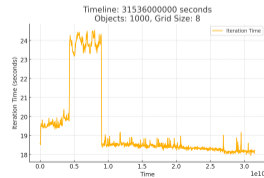
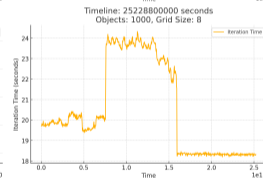
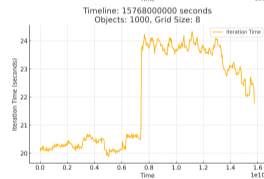
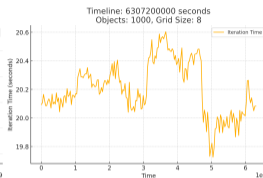
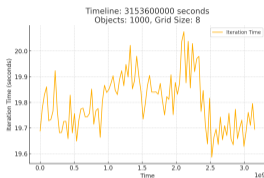


Wikipedia, *Leapfrog integration* — Wikipedia, The Free Encyclopedia

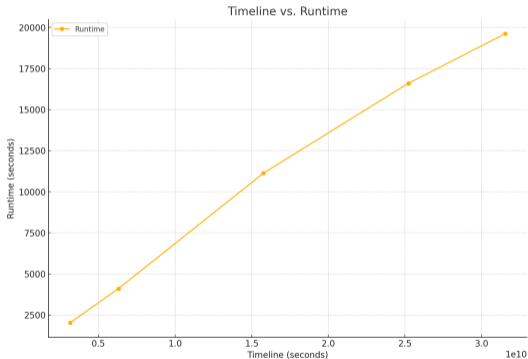
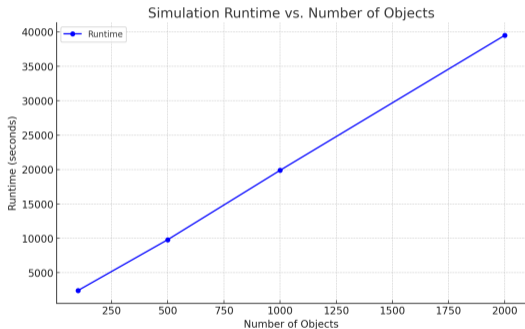
# Performance



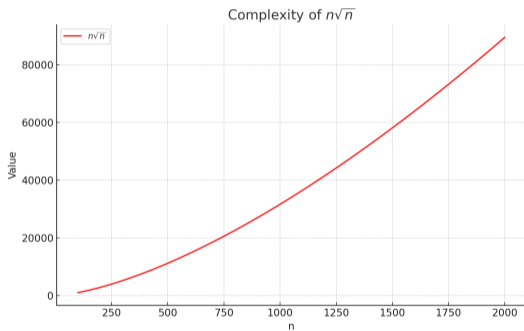
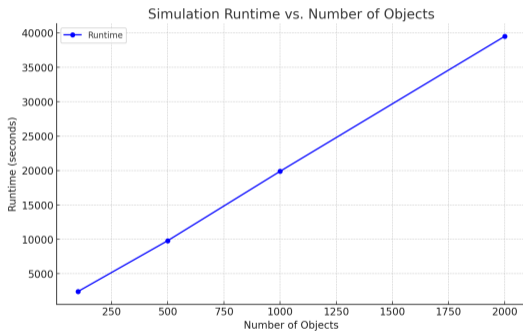
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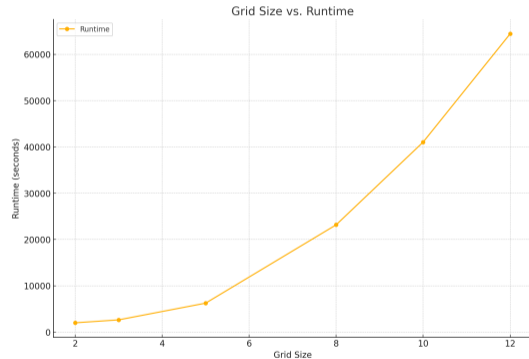


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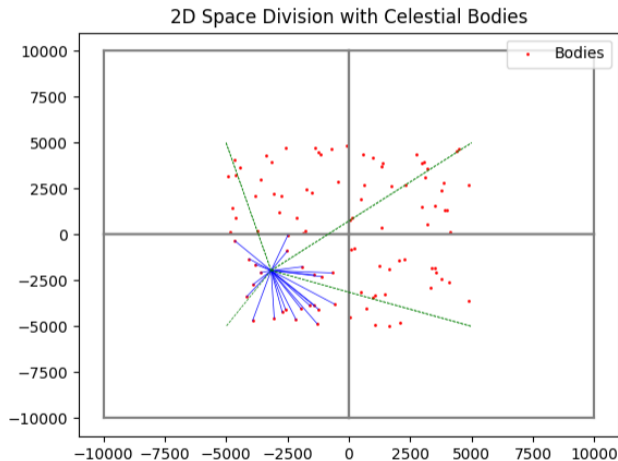
# Performance

- $m = \sqrt{n}$
- $O(\frac{n^2}{m} + nm)$
- $O(n\sqrt{n} + n\sqrt{n})$



# Performance

- $O(\frac{n^2}{m} + nm)$
- $m = n \Rightarrow O(n + n^2)$
- $m = 1 \Rightarrow O(n^2 + n)$
- $\frac{\sqrt{n}}{3} \leq m \leq 3\sqrt{n}$



# Outline

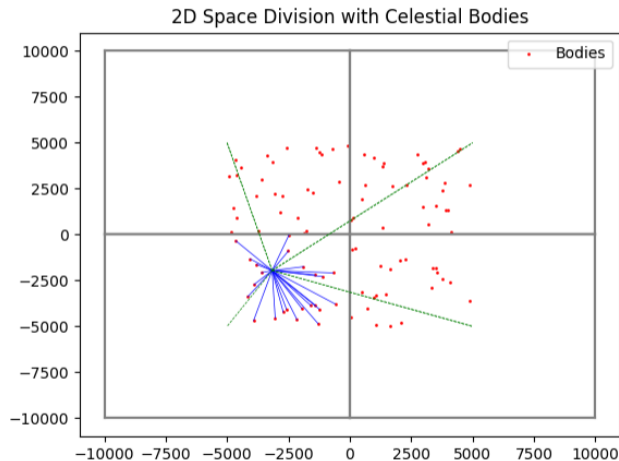
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## Can be Parallel

- Generation / Input read
- Calculation itself - Done
- Object-chunk tracking - Memory intensive
- Output write
- Animation

# Workload Distribution

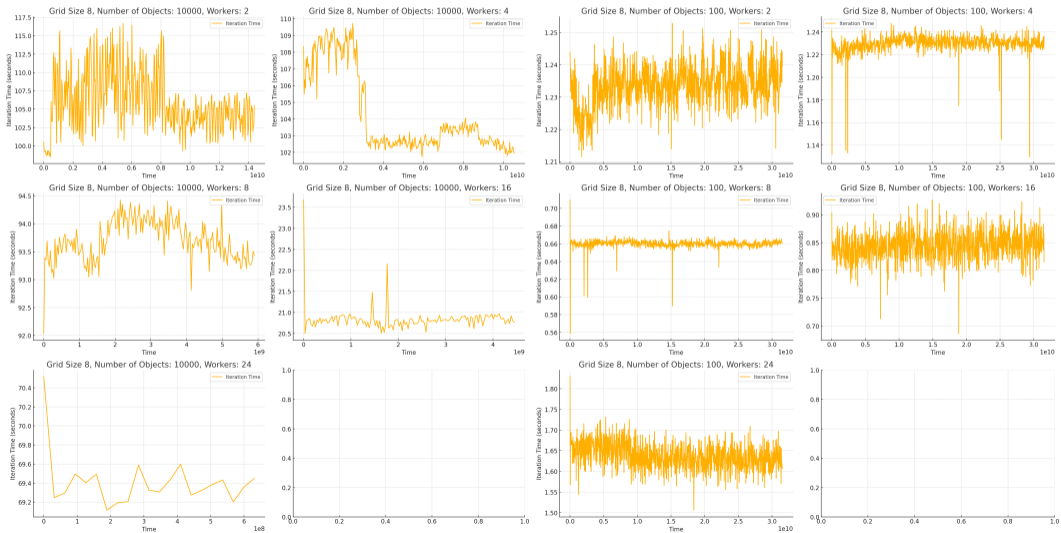
- Chunks can be distributed
- Only total masses and centres are communicated



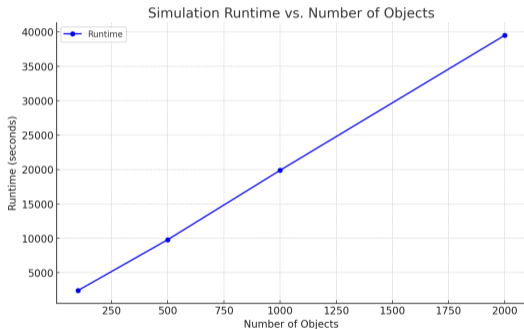
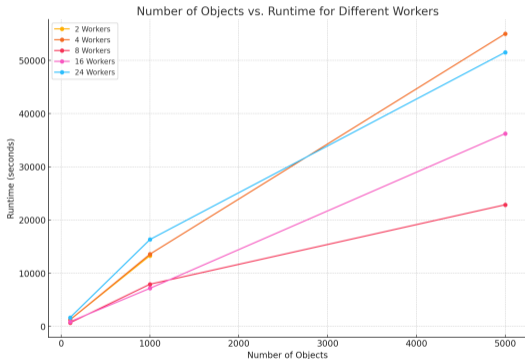
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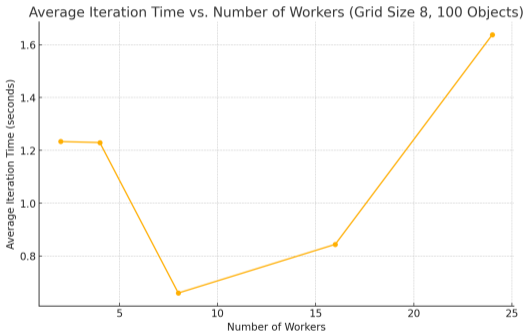
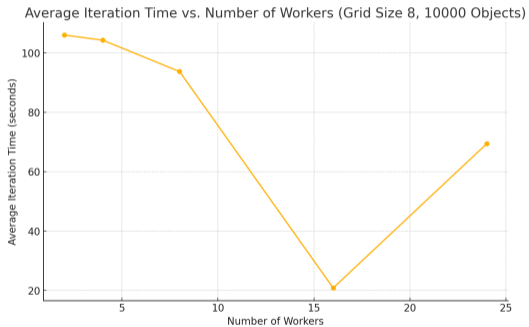
# Performance



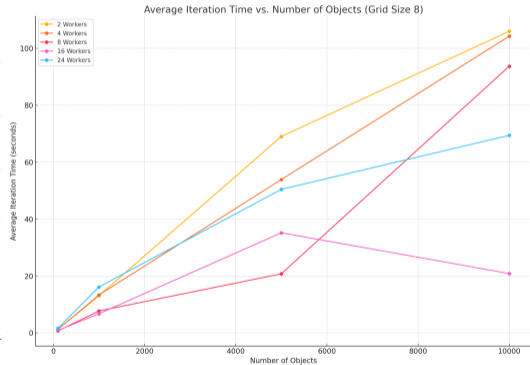
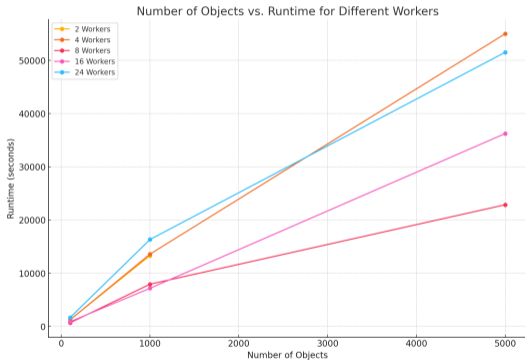
# Comparison to Sequential



# Scaling



# Scaling



# LIKWID Analysis

Shell

```
1 attempt to index a nil value (field '?')
2 stack traceback:
3     .../likwid-mpirun:1952: in function 'printMpiOutput'
4     .../likwid-mpirun:2528: in main chunk
5     [C]: in ?
```

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## Overall Results

- Simulation scales overall good, but can be better
- Optimal number of nodes depends on number of objects and chunks (claim)
- Optimal number of chunks depend on the number of objects
- Real-world scale simulation might not be the best choice

## What is Next

- Checkpoints
- Further scaling analysis
- OctTree parallelization
- Overhead measurement and reduction
- I/O parallelization
- Visualization parallelization
- On node parallelization with multiprocessing library
- Error handling

# References

- Dehnen, W. and J. I. Read. "N-body simulations of gravitational dynamics". In: *The European Physical Journal Plus* 126.5 (May 2011). ISSN: 2190-5444. DOI: 10.1140/epjp/i2011-11055-3. URL: <http://dx.doi.org/10.1140/epjp/i2011-11055-3>.
- Wikipedia. *Leapfrog integration* — *Wikipedia, The Free Encyclopedia*. <http://en.wikipedia.org/w/index.php?title=Leapfrog%20integration&oldid=1220184662>. [Online; accessed 21-June-2024]. 2024.